

## **2012 R3 Annual Meeting, April 30-May 4, Kansas City, MO**

**R3 Project:** The GLM Ground Flash Fraction Retrieval Algorithm: Improvement, Testing, and Demonstration.

**Abstract Title:** The Ground Flash Fraction Retrieval Algorithm Employing Differential Evolution: Simulations and Applications

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### **Abstract**

The ability to estimate the fraction of ground flashes in a set of flashes observed by a satellite lightning imager, such as the future GOES-R Geostationary Lightning Mapper (GLM), would likely improve operational and scientific applications (e.g., severe weather warnings, lightning nitrogen oxides studies, and global electric circuit analyses). A Bayesian inversion method, called the Ground Flash Fraction Retrieval Algorithm (GoFFRA), was recently developed for estimating the ground flash fraction. The method uses a constrained mixed exponential distribution model to describe a particular lightning optical measurement called the Maximum Group Area (MGA). To obtain the optimum model parameters (one of which is the desired ground flash fraction), a scalar function must be minimized. This minimization is difficult because of two problems: (1) Label Switching (LS), and (2) Parameter Identity Theft (PIT). The LS problem is well known in the literature on mixed exponential distributions, and the PIT problem was discovered in this study. Each problem occurs when one allows the numerical minimizer to freely roam through the parameter search space; this allows certain solution parameters to “interchange roles” which leads to fundamental ambiguities, and solution error. A major accomplishment of this study is that we have employed a state-of-the-art genetic-based global optimization algorithm called Differential Evolution (DE) that constrains the parameter search in such a way as to remove both the LS and PIT problems. To test the performance of the GoFFRA when DE is employed, we applied it to analyze simulated MGA datasets that we generated from known mixed exponential distributions. Moreover, we evaluated the GoFFRA/DE method by applying it to analyze actual MGAs derived from low-Earth orbiting lightning imaging sensor data; the actual MGA data were classified as either ground or cloud flash MGAs using National Lightning Detection Network<sup>TM</sup> (NLDN) data. Solution error plots are provided for both the simulations and actual data analyses.



# The Ground Flash Fraction Retrieval Algorithm Employing Differential Evolution: Simulations and Applications

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## 1. GOAL OF R3 PROJECT

When viewing lightning from space at optical wavelengths, the cloud multiple scattering medium obscures the view thereby preventing one from easily determining what flashes strike the ground. However, recent studies have made some progress in estimating the **ground flash fraction**,  $\alpha$ , in a set of  $N$  flashes observed from space [Koshak (2010), Koshak and Solakiewicz (2011), and Koshak (2011)]. Knowledge of  $\alpha$  is important for better understanding:

- Severe Weather,
- Lightning Nitrogen Oxides Chemistry/Climate Studies, and
- Global Electric Circuit.

In the study by Koshak (2011), a Bayesian inversion method was introduced for retrieving the fraction of ground flashes in a set of flashes observed from a (low earth orbiting or geostationary) satellite lightning imager. This method has formed the basis of a Ground Flash Fraction Retrieval Algorithm (GoFFRA) that is being tested as part of GOES-R Geostationary Lightning Mapper (GLM) risk reduction. **Figure 1** summarizes the basic question addressed in this study.

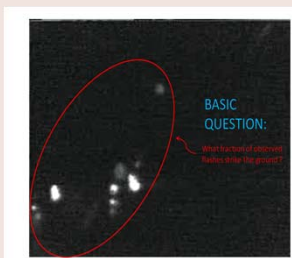


Figure 1. Example of lightning optical emissions as seen from space (STS-52 video).

## 2. THE BAYESIAN RETRIEVAL

**Figure 2** highlights the mathematical attributes of the Bayesian retrieval process. The  $\mu$ 's are the population mean Maximum Group Areas (MGAs) decremented by the nadir footprint area of the space-based lightning imager employed. In summary, the distribution of  $y$  (nadir footprint decremented MGA) is assumed to follow a mixed exponential distribution; one finds the 3 parameters of this distribution that maximizes a scalar function which is a product of probabilities.

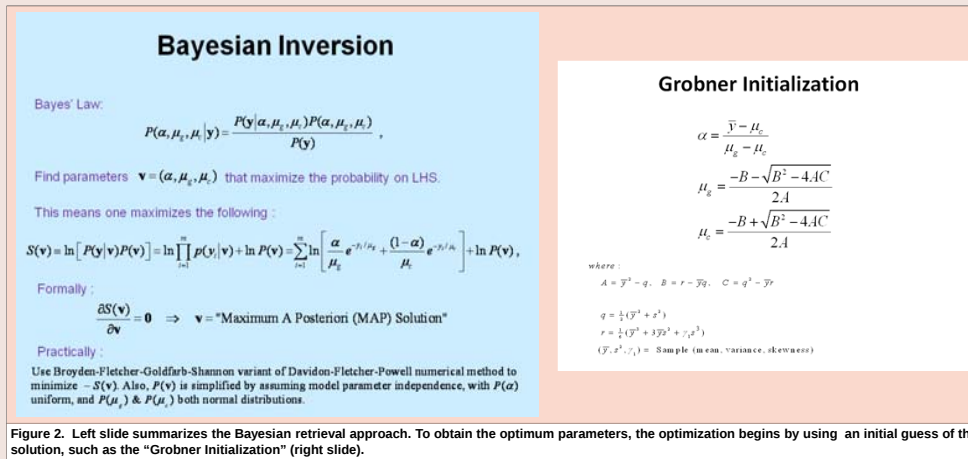


Figure 2. Left slide summarizes the Bayesian retrieval approach. To obtain the optimum parameters, the optimization begins by using an initial guess of the solution, such as the "Grobner Initialization" (right slide).

## 3. ACCOMPLISHMENTS

In addition to developing the Bayesian formalism for the retrieval problem, introducing the use of the mixed exponential model, and deriving the Grobner Initialization, we have conducted preliminary tests of the GoFFRA on simulated datasets. This allowed us to uncover solution errors due to Label Switching (LS) and Parameter Identity Theft (PIT). The LS problem is well known in the literature on mixed exponential distributions, and the PIT problem was discovered in this study. Each problem occurs when one allows the numerical minimizer to freely roam through the parameter search space; this allows certain solution parameters to "interchange roles" which leads to fundamental ambiguities, and solution error. A major accomplishment of this study is that we have employed a state-of-the-art genetic-based global optimization algorithm called Differential Evolution (DE) that constrains the parameter search in such a way as to remove both the LS and PIT problems. We have also applied the GoFFRA/DE method to both simulated and actual MGA datasets (see following section) to evaluate algorithm performance.

## 4. PERFORMANCE TESTS

**a. Simulated Data** To test the performance of the GoFFRA when DE is employed, we applied it to analyze simulated MGA datasets that we generated from known mixed exponential distributions. The solution retrieval errors are provided in **Figure 3**. The retrieval errors are shown as a function of the true ground flash fraction (alpha) of the mixture; vertical lines are standard deviations about the mean retrieval errors. The algorithm performs quite well.

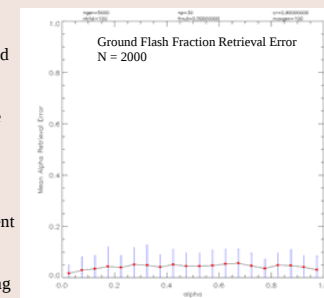


Figure 3. Retrieval errors for simulated data.

**b. OTD Data** Moreover, we evaluated the GoFFRA/DE method by applying it to analyze actual MGAs derived from the low-Earth orbiting lightning imager called the Optical Transient Detector (OTD). The actual MGA data were classified as either ground or cloud flash MGAs using National Lightning Detection Network<sup>TM</sup> (NLDN) data. The ground flash fraction retrieval error plots are provided in **Figure 4**. Errors increase for large alpha (~0.7) indicating a breakdown in the mixed exponential distribution model for the ground flash MGAs. **This is an important finding, as it requires us to upgrade the form of the model to further reduce the retrieval errors.**

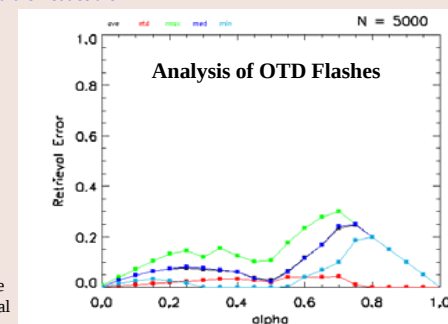


Figure 4. Retrieval errors using mixtures of OTD ground & cloud flashes.

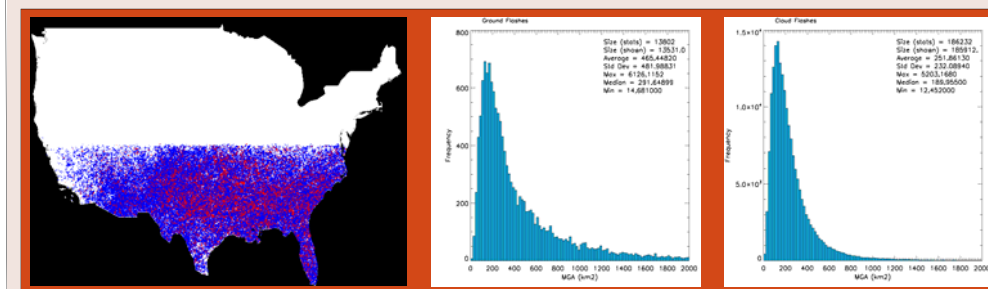


Figure 5. The new test dataset created by comparing 9 yrs of LIS and NLDN data. Leftmost plot is the locations of LIS ground (red) & cloud (blue) flashes.

- **Accomplishments Anticipated @ end of Year 2:** We will upgrade/replace the mixed exponential model, perform retests, and show reduced retrieval errors.
- **Initial Feedback from Potential Users:** Given our results above, we anticipate the start of getting feedback regarding specific GoFFRA applications.
- **What Could be Accomplished w/3<sup>rd</sup> Year Funding:** Completion of additional error analyses showing robustness of algorithm; more elaborate demos.

## 5. REFERENCES

- Koshak, W. J., Optical Characteristics of OTD Flashes and the Implications for Flash-Type Discrimination, J. Atmos. Oceanic Technol., 27, 1822-1838, 2010.
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